

次の関数の導関数を求めよ．

1. $\frac{ax+b}{cx+d}$
2. $x + \sqrt{x^2 + A}$
3. $\sqrt[3]{\frac{x-1}{x+1}}$
4. $\sqrt{x + \sqrt{x^2 + A}}$
5. $\sqrt{\sqrt{x^2 + 1} + \sqrt{x^2 - 1}}$
6. $\log \log x$
7. $\log |x + \sqrt[3]{x^2 + 1}|$
8. $2\sqrt{x}$
9. $x(x+1)^{1/3}(x^2-1)^{-1/2}$
10. $x^{\frac{1}{x}}$
11. x^{x^x}
12. $\frac{\sin x - \cos x}{\sin x + \cos x}$
13. $\log \left| \tan \left(\frac{\pi}{4} + \frac{x}{2} \right) \right|$
14. $(1 + \tan x \tan \frac{x}{2}) \cos x$
15. $\tan^{-1} \frac{1}{x}$
16. $\sin^{-1}(\cos x)$
17. $\sin^{-1}(2x\sqrt{1-x^2})$
18. $\tan^{-1} \sqrt{\frac{1-\cos x}{1+\cos x}}$
19. $x^{\sqrt{x}}$
20. $\log \left| \frac{1 - \sin 2x}{x^x(1 + \sin 2x)} \right|$
21. $x^{\sin x^2}$
22. $e^{\cos(1-3x)} \sin 2x$
23. $\cos^{-1} \left(\frac{e^x - e^{-x}}{e^x + e^{-x}} \right)$
24. $3^{\tan nx}$

n 次導関数はそれぞれ次で与えられることを確かめよ．

1. $(\sin x)^{(n)} = \sin \left(x + \frac{n\pi}{2} \right)$
2. $(\cos x)^{(n)} = \cos \left(x + \frac{n\pi}{2} \right)$
3. $(\log(1+x))^{(n)} = (-1)^{n-1} (n-1)! (1+x)^{-n}$
4. $\left(\frac{1-x}{1+x} \right)^{(n)} = (-1)^n \frac{2n!}{(1+x)^{n+1}}$
5. $(e^x \sin x)^{(n)} = (\sqrt{2})^n e^x \sin \left(x + \frac{n\pi}{4} \right)$
6. $(x^2 e^x)^{(n)} = (x^2 + 2nx + n^2 - n) e^x$